

AN ADULT FEMALE'S HEIGHT CAN BE APPROXIMATED BY THE SQUARE ROOT OF THE PRODUCT OF 23 AND THE LENGTH OF THEIR FOREARM.

$$h = \sqrt{23 \cdot F}$$

A) ABOUT HOW TALL IS A WOMAN WHOSE FOREARM IS 1.4 FT LONG?

$$h = \sqrt{23 \cdot 1.4}$$

$$67(12) = 8''$$

$$h = \sqrt{32.2} = 5.67 \text{ ft}$$

$$5' 8''$$

B) ABOUT HOW LONG IS A WOMAN'S FOREARM IS SHE IS 5'3" TALL?

$$5' 3'' = \sqrt{23 F}$$

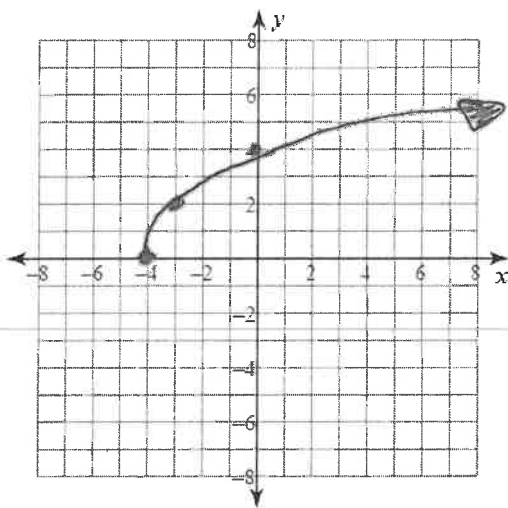
$$\frac{3}{12} = .25 \text{ ft}$$

$$5.25 = \sqrt{23 F}$$

$$\frac{27.0625}{23} = \frac{23 F}{23}$$

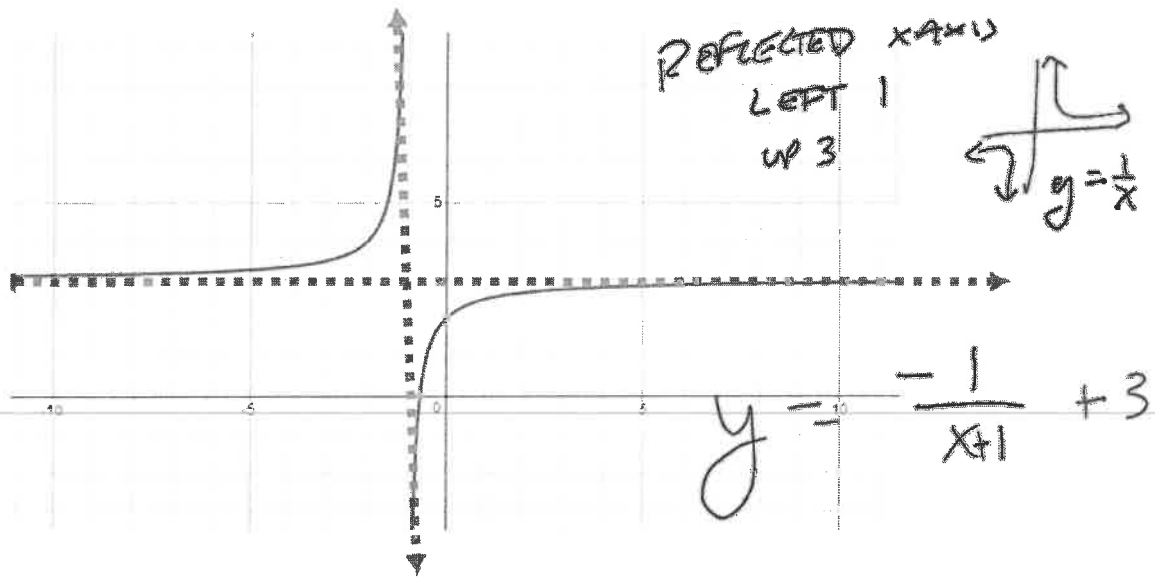
$$F = 1.2 \text{ ft}$$

$$y = 2\sqrt{x+4}$$



LEFT 4

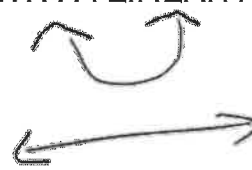
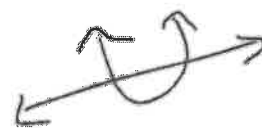
VERTICAL
STRETCH of 2



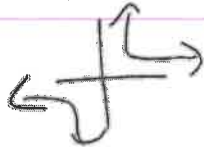
ALWAYS, SOMETIMES, OR NEVER

- THE SOLUTION OF A SYSTEM OF EQUATIONS WITH A LINEAR AND AN QUADRATIC FUNCTION IS TWO POINTS.

SOMETIMES



- THE PARENT FUNCTION OF THE INVERSE VARIATION FUNCTION LIES IN QUADRANTS 1 AND 4.



3

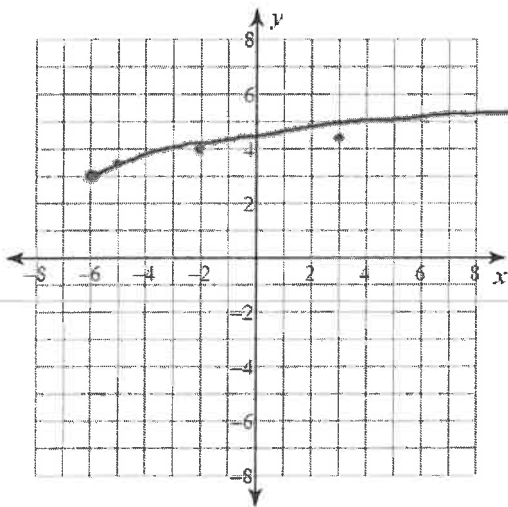
NEVER

$$y = \frac{1}{2}\sqrt{x+6} + 3$$

COMPRESSION OF $\frac{1}{2}$

LEFT 6

UP 3

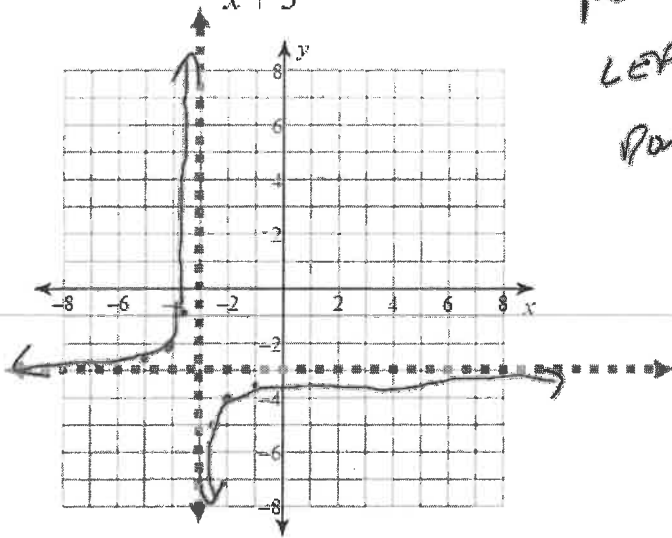


$$f(x) = -\frac{1}{x+3} - 3$$

REFLECT X AXIS

LEFT 3

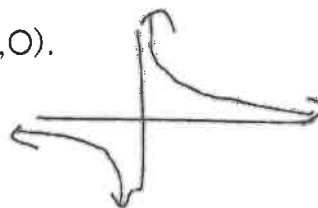
DOWN 3



ALWAYS, SOMETIMES, OR NEVER

- EVERY PARENT GRAPH PASSES THROUGH (0,0).

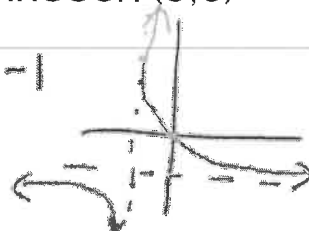
NEVER $y = \frac{1}{x}$ DOES NOT



- INVERSE VARIATION FUNCTIONS CAN GO THROUGH (0,0)

SOMETIMES

$$y = \frac{1}{x+1} - 1$$



SOLVE THE SYSTEM

$$F(x) = 2x - 1$$

$$G(x) = \sqrt{x+1}$$

$$(2x-1)^2 = (2x-1)(2x-1)$$

GCF

$$\boxed{2x-1 = \sqrt{x+1}}$$

$$-1 = \sqrt{1}$$

$$-1 \neq 1$$

$$\underline{(2x-1)^2 = (\sqrt{x+1})^2}$$

$$\begin{array}{r} 4x^2 - 4x + 1 = x + 1 \\ -x \quad -1 \quad -x \quad -1 \end{array}$$

QUAD = 0

$$4x^2 - 5x = 0$$

$$x(4x-5) = 0$$

~~$x = 0$~~

~~$4x-5=0$
 $x = \frac{5}{4}$~~

$$2\left(\frac{5}{4}\right) - 1 \stackrel{?}{=} \sqrt{\frac{5}{4} + 1}$$

$$\frac{10}{4} - 1 \stackrel{?}{=} \sqrt{\frac{9}{4}}$$

$$\frac{3}{2} = \frac{3}{2}$$

$$\sqrt{\frac{5}{4} + \frac{4}{4}}$$

$$\sqrt{\frac{9}{4}}$$

$$\frac{\sqrt{9}}{\sqrt{4}} = \frac{3}{2}$$

$$\sqrt{-9-2n} = \sqrt{2n+27}$$

$$\begin{array}{r} -9-2n = 2n+27 \\ +2n \quad +2n \\ \hline \end{array}$$

$$-9 = 4n + 27$$

$$\begin{array}{r} -27 \quad -27 \\ \hline \end{array}$$

$$-36 = 4n$$

$$\boxed{n=9}$$

$$(x+2)(x+2) = \sqrt{4-x}^2$$

$$x^2 + 4x + 4 = 4 - x$$

$+x$ -4 $-4+x$

$$x+2 = \sqrt{4-x}$$

$$0+2 = \sqrt{4-0}$$

$$2 = 2$$

$$-5+2 = \sqrt{4-5}$$

$$-3 \neq 3$$

$$x^2 + 5x = 0$$

GCF

$$x(x+5) = 0$$

$$x=0$$

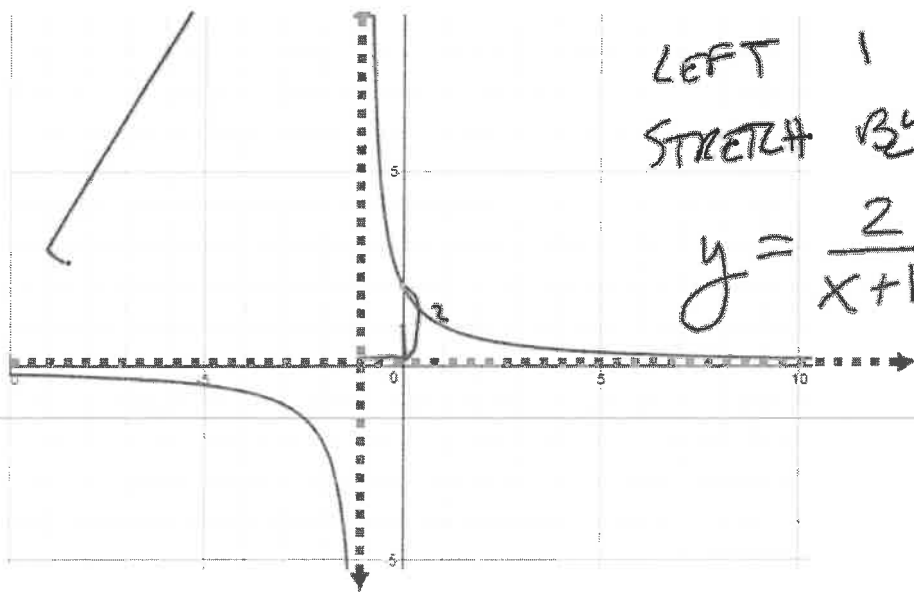
$$x+5=0$$

$$x=-5$$

$$(x+2)(x+2)$$

$$x^2 + 2x + 2x + 4$$

$$x^2 + 4x + 4$$



LEFT 1
STRETCH BY 2

$$y = \frac{2}{x+1}$$

ALWAYS, SOMETIMES, OR NEVER

- $Y = KX$ IS AN INVERSE VARIATION

NEVER

THIS IS DIRECT VARIATION

- THE DOMAIN OF AN INVERSE VARIATION FUNCTION IS $(-\infty, \infty)$.

NEVER



Domain: $(-\infty, 0) \cup (0, \infty)$

SOLVE THE SYSTEM

$$F(x) = x + 3$$

$$G(x) = \frac{4}{x}$$

$$x(x+3) = \left(\frac{4}{x}\right)x$$

$$x^2 + 3x = 4$$

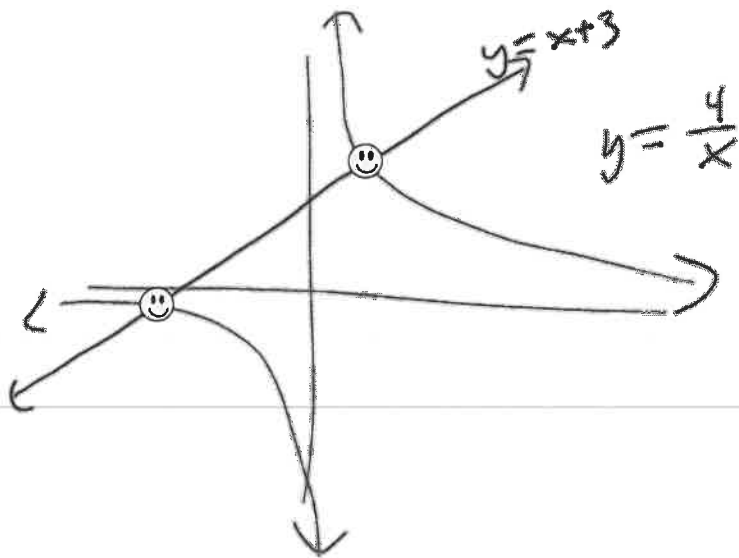
$$\begin{array}{r} -4 \quad -4 \\ \hline \end{array}$$

$$x^2 + 3x - 4 = 0$$

$$(x+4)(x-1) = 0$$

$$x+4=0$$
$$\boxed{x = -4}$$

$$x-1=0$$
$$\boxed{x = 1}$$



$$(n-7)^2 = (\sqrt{22-2n})^2 \quad \text{☺}$$

$$(n-7)(n-7) = 22-2n$$

$$\begin{array}{r} n^2 - 14n + 49 = 22 - 2n \\ + 2n - 22 \quad -22 + 2n \\ \hline \end{array}$$

$$n^2 - 12n + 27 = 0$$

$$(n-9)(n-3) = 0$$

$$\begin{array}{l} n-9=0 \\ \boxed{n=9} \end{array}$$

$$\begin{array}{l} n-3=0 \\ \boxed{n=3} \end{array}$$

$$n-7 = \sqrt{22-2n}$$

$$9-7 = \sqrt{22-2(9)}$$

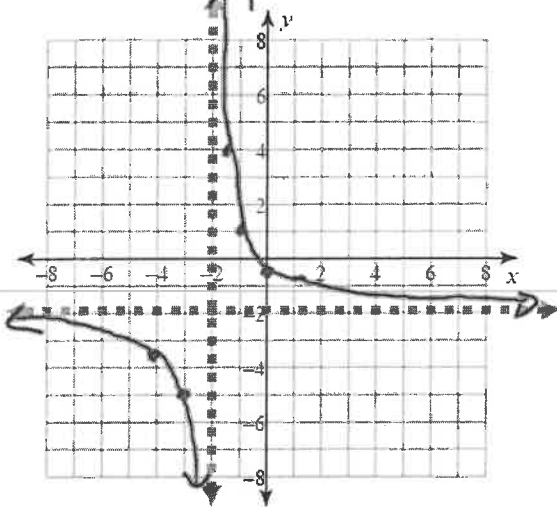
$$2 = \sqrt{4}$$

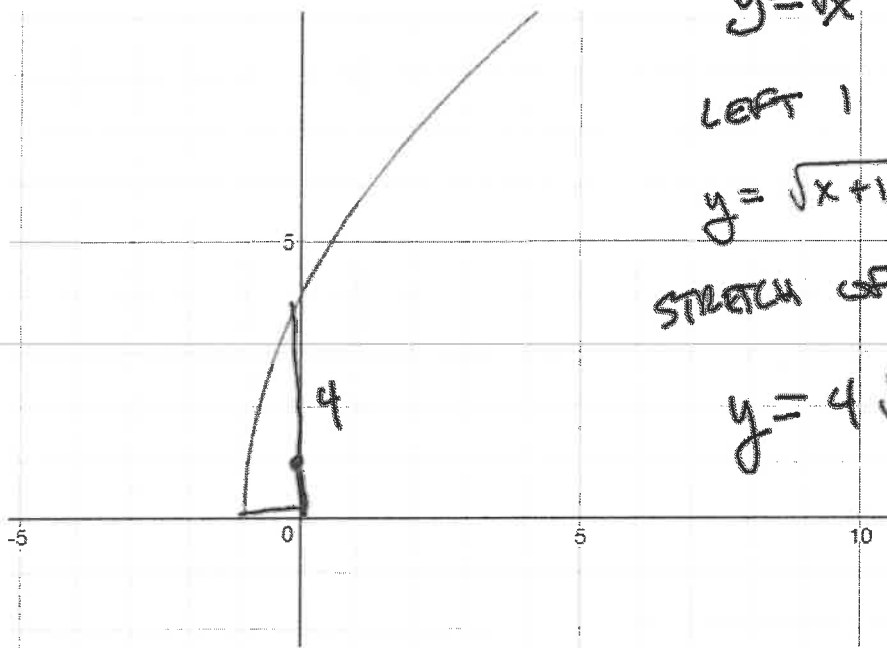
$$3-7 \stackrel{?}{=} \sqrt{22-2(3)}$$

$$-4 \neq 4$$

$$f(x) = \frac{3}{x+2} - 2$$

VERTICAL STRETCH OF 2
LEFT 2
DOWN 2





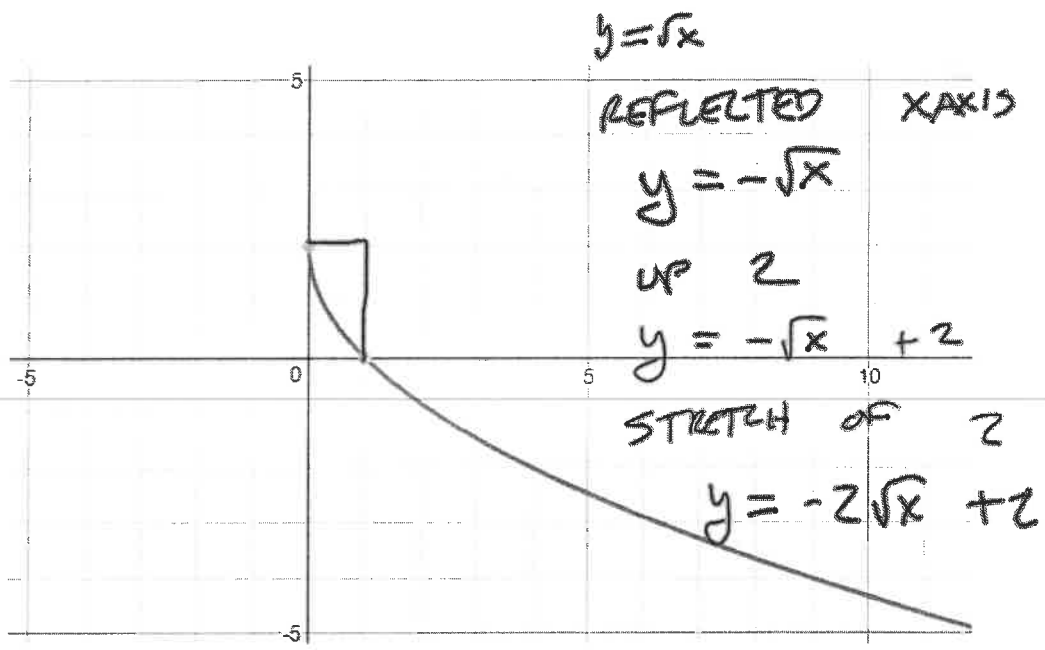
$$y = \sqrt{x}$$

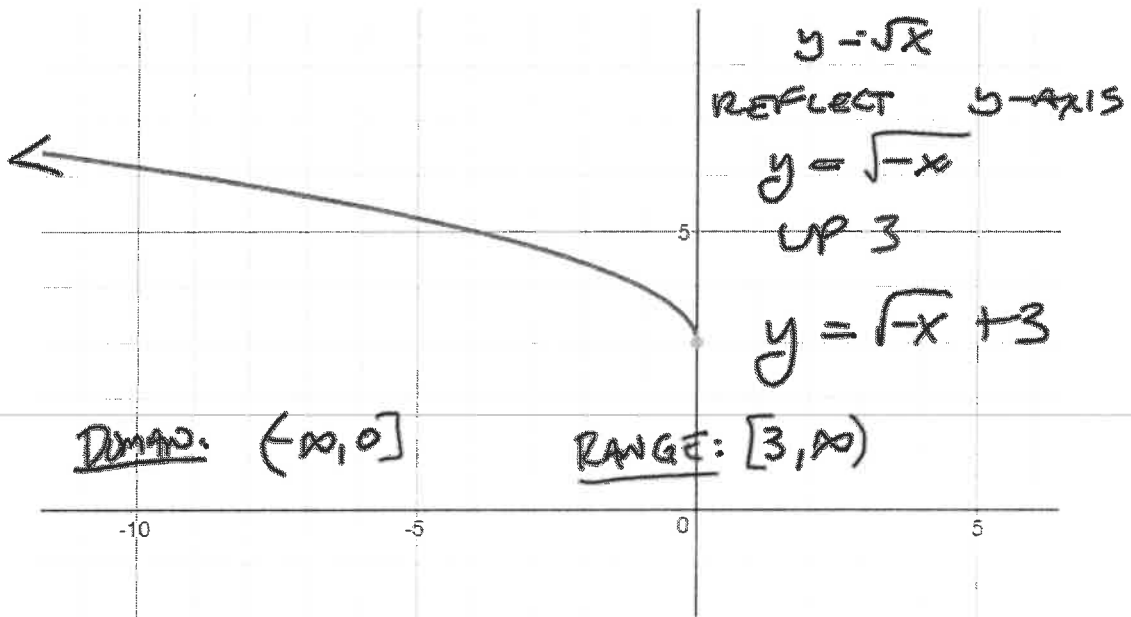
LEFT 1

$$y = \sqrt{x+1}$$

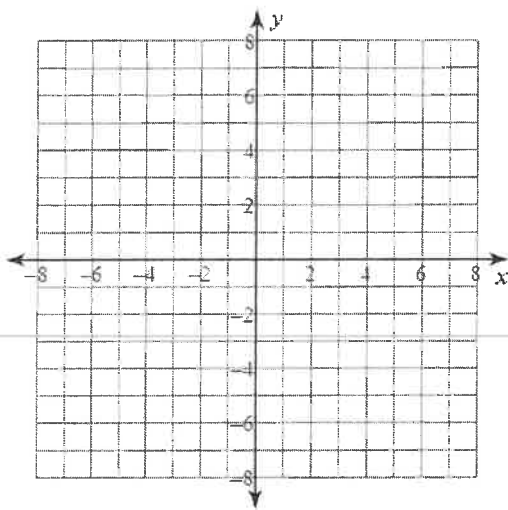
STRETCH OF 4

$$y = 4\sqrt{x+1}$$





$$y = 1 + \sqrt{x+1}$$



Domain: $[-1, \infty)$

$$x+1 \geq 0$$

$$x \geq -1$$

Range: $[1, \infty)$

$$\sqrt{4a+48} - 4 = a$$

+4 +4

$$\sqrt{4a+48} = a+4$$

$$(\sqrt{4a+48})^2 = (a+4)^2$$

$$4a+48 = a^2 + 8a + 16$$

~~-4a~~ ~~-48~~ ~~-4a~~ ~~-48~~

$$0 = a^2 + 4a - 32$$

$$0 = (a+8)(a-4)$$

$$a+8=0$$

~~a = -8~~

$$a-4=0$$

$\boxed{a=4}$

Check:

$$\textcircled{-8} \quad \sqrt{4(-8)+48} - 4 \stackrel{?}{=} -8$$

$$\sqrt{-32+48} = 4$$

$$\sqrt{16} = 4$$

$$4-4 = -8$$

$$0 \neq -8$$

$$\textcircled{4} \quad \sqrt{4 \cdot 4 + 48} - 4 = 4$$

$$\sqrt{16+48} - 4 = 4$$

$$\sqrt{64} - 4 = 4$$

$$8-4=4$$

✓

$$\sqrt{14-5x} = x$$

$$(\sqrt{14-5x})^2 = (x)^2$$

$$\begin{array}{r} 14-5x = x^2 \\ -14+5x \quad +5x-14 \end{array}$$

$$0 = x^2 + 5x - 14$$

$$0 = (x+7)(x-2)$$

$$\cancel{x = -7} \text{ or } \boxed{x = 2}$$

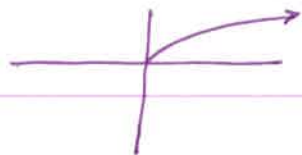
$$\begin{array}{l} (-7) \sqrt{14-5(-7)} = -7 \\ \sqrt{14+35} = -7 \\ \sqrt{49} \neq -7 \end{array}$$

$$\sqrt{14-5(2)} = 2$$

$$\begin{array}{l} \sqrt{14-10} = 2 \\ \sqrt{4} = 2 \end{array}$$

ALWAYS, SOMETIMES, OR NEVER

- THE RANGE OF A SQUARE ROOT FUNCTION IS $(-\infty, 0]$ *Sometimes*

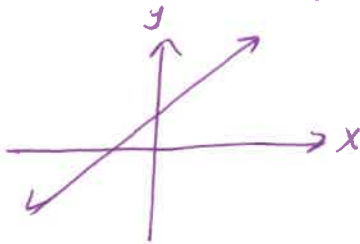


$$R = [0, \infty)$$

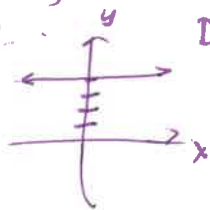


$$R = (-\infty, 0]$$

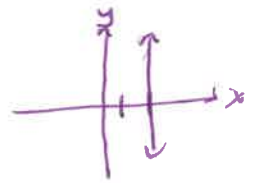
- THE DOMAIN AND RANGE OF A LINEAR FUNCTION IS $(-\infty, \infty)$ *Sometimes*



$$D = (-\infty, \infty)$$
$$R = (-\infty, \infty)$$



$$D = (-\infty, \infty)$$
$$R = [4]$$



$$D = [2]$$
$$R = (-\infty, \infty)$$

$$\frac{3}{x} = 2x + 1$$

$$\frac{3}{x} = \frac{2x+1}{1}$$

$$x(2x+1) = 3$$

$$2x^2 + x = 3$$

$$2x^2 + x - 3 = 0$$

$$(2x + 3)(x - 1) = 0$$

$$2x + 3 = 0$$

$$x - 1 = 0$$

$$2x = -3$$

$$x = 1$$

$$x = \frac{-3}{2}$$

$$\left(\frac{-3}{2}\right)$$

$$\frac{3}{\frac{-3}{2}} = 2\left(\frac{-3}{2}\right) + 1$$

$$3 \cdot \frac{2}{-3} = -3 + 1$$

$$= -2 = -2 \quad \checkmark$$

①

$$\frac{3}{1} = 2(1) + 1$$

$$3 = 2 + 1 \quad \checkmark$$

I

IT TAKES FIVE PEOPLE THREE HOURS TO PAINT A ROOM. HOW MANY MORE MINUTES WOULD IT TAKE FOUR PEOPLE TO PAINT THE ROOM?

$$y = \frac{k}{x}$$

$$t = \frac{k}{p}$$

I

$$3 = \frac{k}{5}$$

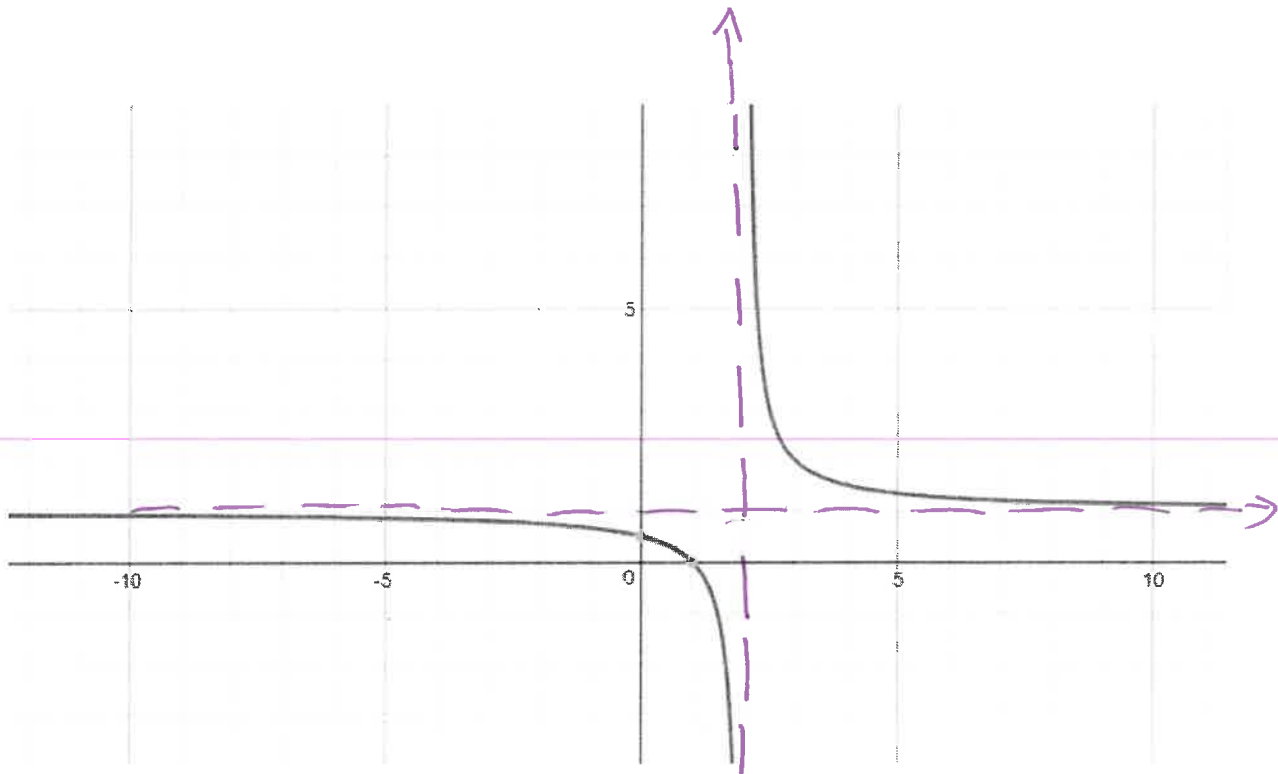
$$k = 15$$

4

$$T = \frac{15}{4}$$

$$T = 3.75 \text{ (3 hrs. 45 min)}$$

- It took 4 people 45 minutes longer than it took 5 people.



$$y = \frac{1}{x-2} + 1$$

right 2
hyp. 1
no stretch
no flip